



Original

Ti-5Al-5Mo-5V-3Cr and similar Mo equivalent alloys: First principles calculations and experimental investigations

Premkumar Manda^a, Ashish Pathak^a, A. Mukhopadhyay^a, Uday Chakkingal^b, A.K. Singh^{a,*}

^a Defence Metallurgical Research Laboratory, Kanchanbagh P.O., Hyderabad 500058, India

^b Department of Metallurgical and Materials Engineering, Indian Institute of Technology Madras, Chennai 600 036, India

Received 26 May 2016; accepted 4 November 2016

Available online 14 February 2017

Abstract

This paper reports the stability of Ti-5Al-5Mo-5V-3Cr and similar Mo equivalent alloys using first principles calculations. The lattice constant and modulus values are calculated using X-ray diffraction and ultrasonic techniques, respectively. All the four alloys display negative values of formation energy per atom and the alloy Ti-5Al-5Mo-5V-3Cr is most stable among these. The lattice constant, modulus and hardness values of these alloys lie in low (Ti-5Al-5Mo-5V-3Cr, Ti-5Al-5Mo-8.6V-1.5Cr) and high (Ti-5Al-3.5Mo-7.2V-3Cr, Ti-5Al-3.5Mo-5V-3.94Cr) regimes. All the alloys display ductile behavior based on shear and bulk modulus ratios.

© 2017 Universidad Nacional Autónoma de México, Centro de Ciencias Aplicadas y Desarrollo Tecnológico. This is an open access article under the CC BY-NC-ND license (<http://creativecommons.org/licenses/by-nc-nd/4.0/>).

Keywords: Ti-5Al-5Mo-5V-3Cr; First principles; X-ray diffraction; Transmission electron microscopy

1. Introduction

The development of β titanium alloys have been focussed in aerospace industries during last two decades due to their attractive properties such as high strength, fracture toughness, fatigue properties, deep hardenability and reasonable ductility (Boyer & Briggs, 2005; Fanning, Nyakana, Patterson, & McDaniel, 2007; Ghosh, Sivaprasad, Bhattacharjee, & Kar, 2013; Jones, Dashwood, Jackson, & Dye, 2009b; Shekhar, Sarkar, Kar, & Bhattacharjee, 2015). These alloys can be classified as metastable and stable β alloys. The α phase can be retained in former alloys in different heat treated conditions. As a result, a variety of microstructures can be produced with different combinations of solution treatment and aging. These are in turn useful to tailor the mechanical properties. For example, fine distribution of α precipitates particularly in metastable β titanium alloys provides high strength due to large number of α/β phase boundaries. These boundaries act as dislocation barriers

(Collings, 1984; Dehghan-Manshadi & Dippenaar, 2011; Duerig & Williams, 1983; Jones, Dashwood, Jackson, & Dye, 2009a).

The metastable β titanium Ti-5Al-5Mo-5V-3Cr (Ti-5553) (wt.%) alloy has been developed recently to replace the alloy Ti-10V-2Fe-3Al (Ti-1023) in some of the structural components of the aircraft. The microstructure, texture and mechanical properties of the alloy Ti-5553 and similar Mo equivalent (8.15) (Weiss & Semiatin, 1998) have been investigated in detail in hot rolled condition (Manda, Chakkingal, & Singh, 2014; Manda, Ghosal, Chakkingal, & Singh, 2015; Manda, Chakkingal, & Singh, 2016). The Mo equivalent is defined as the sum of the weighted averages of the elements (wt.%) present in alloy (Weiss & Semiatin, 1998). This is given as

$$\text{Mo}_{\text{eq}} = \text{Mo} + 0.67\text{V} + 0.44\text{W} + 0.28\text{Nb} + 0.22\text{Ta} + 1.6\text{Cr} + 1.25\text{Ni} + 1.7\text{Co} + 2.9\text{Fe} - 1.0\text{Al} \quad (\text{wt.}\%) \quad (1)$$

Present work is mainly focussed on the relative stability of β phase in these alloys using first principles calculations. The equilibrium lattice constant values have been compared with the lattice constant values calculated from X-ray diffraction (XRD) data. The elastic constants of these alloys are also evaluated using conventional ultrasonic method.

* Corresponding author.

E-mail address: singh.ashok3@rediffmail.com (A.K. Singh).

Peer Review under the responsibility of Universidad Nacional Autónoma de México.

Table 1
Chemical composition of the experimental alloys.

Alloy designation	Nominal composition (wt.%)				Analyzed composition (wt.%)				Interstitial elements (wt.%)			
	Al	Mo	V	Cr	Al	Mo	V	Cr	C	O	N	H
A1	5.0	5.0	5.0	3.0	5.17	4.96	4.85	2.98	0.021	0.10	0.007	0.016
A2	5.0	3.5	7.2	3.0	5.10	3.30	7.30	3.20	0.075	0.04	0.017	0.012
A3	5.0	5.0	8.6	1.5	5.25	4.52	8.75	1.50	0.025	0.12	0.005	0.005
A4	5.0	3.5	5.0	3.9	5.41	3.18	5.25	4.16	0.035	0.13	0.005	0.005

2. Experimental details

The details of the melting procedure of four experimental alloys with nominal compositions Ti-5Al-5Mo-5V-3Cr, Ti-5Al-3.5Mo-7.2V-3Cr, Ti-5Al-5Mo-8.6V-1.5Cr and Ti-5Al-3.5Mo-5V-3.94Cr designated as A1, A2, A3 and A4, respectively are given elsewhere (Manda et al., 2015). The chemical composition of alloy A1 is same as the Ti-5553, while the other three alloys (A2, A3 and A4) were selected by keeping Mo equivalent constant (8.15) with different combinations of Mo, V and Cr. The analyzed chemical compositions of all four alloys are given in Table 1. The as-cast alloys were solution treated in β phase field and subsequently water quenched (β WQ). The densities of all the alloys have been measured using Archimedes principle. The β WQ samples for microscopy were prepared following standard metallographic techniques used for titanium and its alloys and etched with modified Kroll's reagent [94 ml H_2O , 4 ml HNO_3 and 2 ml HF]. The microstructures of β WQ samples were examined using optical and scanning electron microscopes (OM and SEM). The corresponding XRD patterns were recorded using a Philips PW3020 diffractometer equipped with a graphite monochromator operated at 40 kV and 25 mA. Transmission electron microscopy (TEM) samples were prepared using standard techniques and TEM was performed using a FEI TECNAI G^2 microscope. The elastic constants were measured by using ultrasonic longitudinal and transverse wave velocities. Ultrasonic velocities were measured using a 200 MHz pulser receiver (Olympus NDT Panametrics PR 5900) with a 10 MHz transducer for longitudinal and 5 MHz transducer for the transverse wave velocities. The signal was digitized at 1 Gs/s rate using an analog to digital converter card. Five measurements were made for each sample and average values are reported. Vicker's hardness number (VHN) values were measured using the AFFRI hardness tester (model: VRSD 270).

3. Computational details

In present study, the ABINIT software having first principles norm conserving pseudo potential method in the frame work of the density functional theory (DFT) has been utilized (Gonze et al., 2002, 2009; Hohenberg & Kohn, 1964; Kohn & Sham, 1965). Exchange-correlation effects have been treated within generalized gradient approximation (GGA) using Perdew–Burke–Ernzerhof formulation (Perdew, Burke, & Ernzerhof, 1996). For all the alloys, convergence with respect to the plane wave cut-off energy has been verified and accordingly plane wave cut-off energy of 40 Ry has been used. Subsequently,

conversions of wave functions between real and reciprocal lattices have been carried out using fast Fourier transform algorithm (Goedecker, 1997). Accordingly, conjugate gradient algorithm (Gonze, 1996; Payne, Teter, Allan, Arias, & Joannopoulos, 1992) has been employed within the frame work of self-consistency. The integration over the Brillouin zone (BZ) has been done with the Monkhorst–Pack scheme (Monkhorst & Pack, 1976). The convergence with respect to k-points has been checked for all the alloys and the optimum value used for the present calculations is $6 \times 6 \times 6$. The periodic boundary conditions (PBCs) have been considered along $\langle 100 \rangle$, $\langle 010 \rangle$ and $\langle 001 \rangle$ crystallographic directions. The structural optimizations of all the three phases for obtaining the minimum energies have been performed by relaxing the lattice constants. Convergence in present calculation has been obtained when the differences between energies and forces in two consecutive steps are less than 1.36×10^{-4} meV and 0.36 eV/Å, respectively.

The number of atoms considered for β phase of the alloy Ti-5553 (A1) in present calculation is 128. Both the formation energy per atom and the lattice constants have been computed and given in Table 2. The formation energy per atom has been defined as

$$E_{\text{for}} = \frac{1}{(u + v + x + y + z)} \times (E_{\text{Ti-5553}} - uE_{\text{Ti}}^g - vE_{\text{Al}}^g - xE_{\text{Mo}}^g - yE_{\text{V}}^g - zE_{\text{Cr}}^g) \quad (2)$$

where $E_{\text{Ti-5553}}$ is the total system energy of Ti-5553 alloy having u Ti, v Al, x Mo, y V and z Cr atoms, E_{Ti}^g , E_{Al}^g , E_{Mo}^g , E_{V}^g and E_{Cr}^g are the total energy per atom in their ground states for Ti, Al, Mo, V and Cr atoms, respectively and $(u + v + x + y + z)$ denotes the total number of atoms considered in the unit cell. Eq. (2) is written for the alloy A1 and can be suitably modified for other three alloys (A2, A3 and A4) depending upon their chemical compositions.

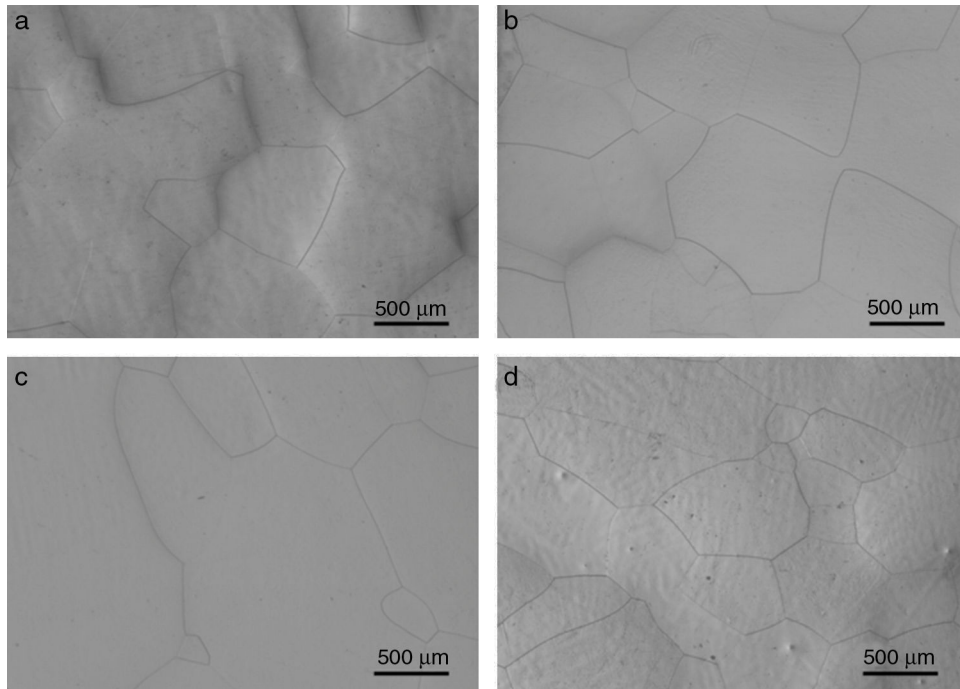
4. Results and discussion

The densities of all the four alloys measured by Archimedes principle are given in Table 2. These are highest and lowest for the alloys A3 and A4, respectively. The highest value of the density for alloy A3 can be attributed to presence of 5 wt.% Mo and 8.6 wt.% Cr. It is to be noted that the densities of Mo and Cr are 10.2 and 7.2 g/cc, respectively. The lowest value of density of the alloy A4 on the other hand can be attributed to low wt.% of Mo (3.5) along with Cr (3.94).

Table 2

Equilibrium lattice constants and formation energy per atom for all the four alloys A1, A2, A3 and A4.

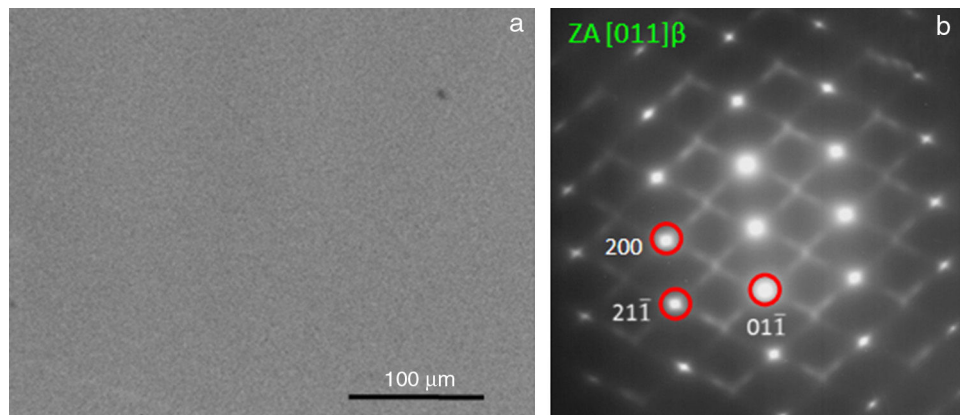
Alloy designation	Density (g/cc)	Lattice constants (Å)		Formation energy per atom (eV)
		Experimental	First principles calculation	
A1	4.635	3.2357	3.1949	−0.0018
A2	4.645	3.2493	3.1973	−0.0016
A3	4.659	3.2366	3.1966	−0.0017
A4	4.587	3.2445	3.1967	−0.0015

Fig. 1. Optical microstructures of β WQ specimens: (a) A1, (b) A2, (c) A3 and (d) A4.

The optical microstructures of all the four alloys in β WQ condition are shown in Figure 1. This clearly exhibits the presence of single phase. This has been confirmed by back scattered electron (BSE) image of these alloys. A representative BSE microstructure of the alloy A1 along with the selected area electron diffraction (SAED) obtained by TEM is given in Figure 2. The SAED patterns of all four alloys exhibit the presence of single

β phase. The XRD patterns (Fig. 3) of these alloys also confirm the presence of single β phase in β WQ condition. The crystallographic details of the β phase are given in Table 3. The lattice constant ‘a’ of these alloys has been calculated from corresponding XRD patterns using Celn method and given in Table 2.

The lattice constant ‘a’ values of all the alloys are smaller than the distinctive β titanium (3.283 Å, from JCPDS: 89-4913)

Fig. 2. β WQ specimen of the alloy A1: (a) BSE-SEM and (b) SAED pattern showing $[110]\beta$ zone axis.

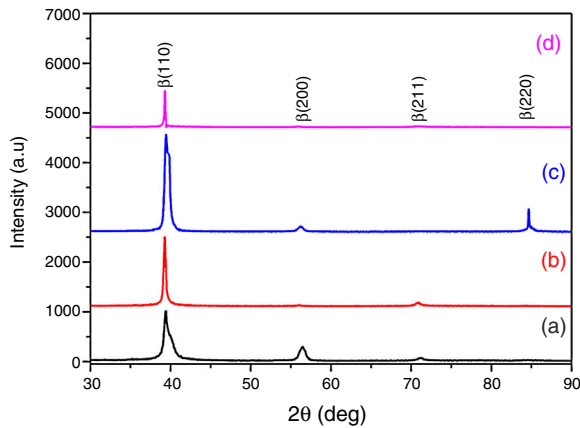


Fig. 3. XRD patterns of β WQ specimens: (a) A1, (b) A2, (c) A3 and (d) A4 in β WQ condition.

(Levinger, 1953). The lattice constant values of alloys A1 and A2 are comparatively lower than those of the A3 and A4. This can be ascribed to the presence of alloying elements of these alloys having smaller atomic radii compared to pure titanium (1.47 Å). The atomic radii of the other alloying elements are Al (1.43 Å), Mo (1.39 Å), V (1.34 Å) and Cr (1.28 Å) (Takeuchi & Inoue, 2005). The wt.% of alloying elements and corresponding sizes of the atoms also explain the variation in lattice constant values.

The SAED patterns of all the four alloys show streaks. A representative SAED pattern of the alloy A1 is shown in Figure 2b. These points toward the instability of microstructures in β WQ condition due to presence of a very fine distribution of athermal ω phase. It is to be noted that this phase cannot be detected by XRD and SEM due to small volume fraction and very small size (2–5 nm). This is quite common in β WQ metastable β titanium alloys and fine precipitation of ω phase occurs irrespective of the cooling rate from the corresponding β phase field (Nag, 2008).

The formation energy per atom values of all the alloys obtained by first principles calculation and corresponding lattice constants are given in Table 2. These values lie in the similar range to those reported for β titanium alloys (Dai, Wu, Song, & Yang, 2012). All the alloys display low negative values of formation energy per atom and the increasing order is A1, A3, A2 and A4. This clearly indicates that all the alloys are energetically stable and the alloy A1 is most stable among all the alloys. The order of formation energy per atom values observed in present study is not surprising since alloys A1 and A3 contain maximum

Mo content. It is important to mention here that the Mo is the strong β stabilizer among all the β stabilizing elements.

The equilibrium lattice constant values of all the four alloys are obtained from formation energy per atom vs a curves (Table 2). These values are lower than those obtained by XRD patterns of the β WQ samples. This can be attributed to the state of β WQ samples which have been water quenched from 900 °C to room temperature. Therefore, these values represent the lattice parameter values at 900 °C while equilibrium lattice constant values obtained by first principles calculations at 0 K (–273 °C).

These alloys contain five elements which require very large unit cell to compute modulus values. This also needs a large computation time. Consequently, the modulus and Poisson's ratio values of these alloys were computed using ultrasonic longitudinal and transverse wave velocities using the following equations.

$$E = \frac{3\rho V_T^2 \{V_L^2 - (4/3 * V_T^2)\}}{V_L^2 - V_T^2} \quad (3)$$

$$\nu = \frac{V_L^2 - 2V_T^2}{2(V_L^2 - V_T^2)} \quad (4)$$

where E , ρ , V_T , V_L and ν are Young's modulus, density, transverse ultrasonic wave velocity, longitudinal ultrasonic wave velocity and Poisson's ratio, respectively. Eqs. (3) and (4) have been used to calculate Young's modulus and Poisson's ratio and given in Table 4. The values of Poisson's ratio obtained in present study are close to other metastable β titanium alloys (Gerday, 2009).

It appears that the modulus values lie in two regimes, i.e. lower (A1, A3) and higher (A2, A4). The Poisson's ratios on the other hand display opposite trend to those of modulus values. The ratio of shear and bulk modulus values can be utilized to predict the brittle and ductile behavior of materials (Pugh, 1954). The ratio G/B (shear/bulk modulus) > 0.57 is associated with brittle otherwise related with ductile behavior. The G/B ratios of the present alloys are less than 0.57 and indicate that these alloys are ductile. Premkumar et al. have recently investigated the mechanical behavior of these alloys in hot rolled condition and observed that these alloys display reasonable ductility (Manda et al., 2016). These results are in good agreement with the calculated G/B ratios in the present study. On the other hand, the values of Poisson's ratios obtained in present study are less than 0.33 which reflect that these alloys are brittle (Frantsevich, Voronov, Bokuta, & Frantsevich, 1983). The values of Poisson's ratio of these alloys lie in the range of metallic materials. Therefore, the nature of bonding force between atoms is metallic. The opposite trend obtained by G/B and Poisson's ratios can therefore be attributed to metastable condition of the alloys.

The VHN values surprisingly also follows similar trend to those of modulus values and lies in lower and higher regimes. The hardness values of alloys A2 and A4 (measured at 10 kg load) are higher than those of A1 and A3. It is to be noted that the lattice constants of these alloys also lies in two regimes i.e. lower (A1, A3) and higher (A2, A4 regimes). The high hardness of alloy A2 can be attributed to solid solution effect of

Table 3
Crystallographic data for present experimental alloys.

Disordered: cubic					
$Im\bar{3}m$ or O_h^2 ; 2 atoms per unit cell					
cI2					
Atomic positions:					
Atoms	Wyckoff notation	Symmetry	x	y	z
Ti/Al/Mo/V/Cr	2(a)	m3m	0	0	0
The sum of the addition of probabilities of the Ti (P_{Ti}),					
Al (P_{Al}), Mo (P_{Mo}), V (P_V) and Cr (P_{Cr}) atoms on					
2(a) sites is 1.					

Table 4

Young's modulus (E), Poisson's ratio, bulk modulus (B), shear modulus (G), G/B and Vickers hardness number (VHN) at 10 kg load for all the four alloys A1, A2, A3 and A4.

Alloy designation	E (GPa)	ν	B (GPa)	G (GPa)	G/B	Vickers hardness number (VHN) at 10 kg load
A1	110 $\pm$ 5	0.285	85	43	0.506	298 $\pm$ 2.5
A2	126 $\pm$ 5	0.270	91	50	0.516	317 $\pm$ 2.0
A3	115 $\pm$ 5	0.280	87	45	0.517	293 $\pm$ 4.0
A4	125 $\pm$ 5	0.275	93	49	0.516	304 $\pm$ 2.5

alloying elements (Mo, V and Cr) on the single β phase. The solid solution effect is more predominant in A2 exhibiting both higher lattice constants and the higher VHN values. The variation in bulk modulus values of the present alloys is small due to small variation in lattice constants. In addition, the measurement of bulk modulus has been carried out in β WQ condition which is in metastable condition. Therefore, a correlation among lattice constants, hardness and bulk modulus values is rather inappropriate. However, it appears that the presence of solute atoms has same effect on modulus, VHN and lattice constant values.

5. Conclusions

1. All the four alloys (Ti-5Al-5Mo-5V-3Cr, Ti-5Al-3.5Mo-7.2V-3Cr, Ti-5Al-5Mo-8.6V-1.5Cr and Ti-5Al-3.5Mo-5V-3.94Cr) display negative values of formation energy per atom and the alloy Ti-5Al-5Mo-5V-3Cr is most stable among these.
2. The lattice constant, modulus and hardness values of these alloys lie in lower (Ti-5Al-5Mo-5V-3Cr, Ti-5Al-5Mo-8.6V-1.5Cr) and higher (Ti-5Al-3.5Mo-7.2V-3Cr, Ti-5Al-3.5Mo-5V-3.94Cr) regimes.
3. All the alloys display ductile behavior based on shear and bulk modulus ratios.

Conflict of interest

The authors have no conflicts of interest to declare.

Acknowledgements

The authors wish to acknowledge Defence Research and Development Organization for financial support. We are grateful to Dr. Samir V. Kamat, Director, Defence Metallurgical Research Laboratory for his kind encouragement. Director ANURAG, Hyderabad and Shri A. Mondal are gratefully acknowledged for the provision of computational facilities and Dr. R. Sankarasubramanian for his kind support. Authors also thank Electron Microscopy, Titanium Alloy Groups of DMRL.

References

- Boyer, R. R., & Briggs, R. D. (2005). The use of β titanium alloys in the aerospace industry. *Journal of Materials Engineering and Performance*, 14(6), 681–685.

- Collings, E. W. (1984). *Physical metallurgy of titanium alloys*. pp. 261. OH, USA: American Society of Metals.
- Dai, J. H., Wu, X., Song, Y., & Yang, R. (2012). Electronic structure mechanism of martensitic phase transformation in binary titanium alloys. *Journal of Applied Physics*, 112(12), 123718-1-9.
- Dehghan-Manshadi, A., & Dippenaar, R. J. (2011). Development of α -phase morphologies during low temperature isothermal heat treatment of a Ti-5Al-5Mo-5V-3Cr alloy. *Materials Science and Engineering: A*, 528(3), 1833–1839.
- Duerig, T. W., & Williams, J. C. (1983). Overview, microstructure and properties of beta titanium alloys. In R. R. Boyer, & H. W. Rosenberg (Eds.), *Beta titanium alloys in the 1980's* (Vol. 1984) (pp. 19–68). Warrendale, PA: TMS of AIME.
- Fanning, J. C., Nyakana, S. L., Patterson, K. M., & McDaniel. (2007). Heat treatment, microstructure and properties of TIMETAL 555. In M. Niinomi, S. Akiyama, M. Hagiwara, M. Ikeda, & K. Maruyama (Eds.), *Titanium: Science and technology* (pp. 499–502). Kyoto, Japan: JIMIC.
- Frantsevich, I. N., Voronov, F. F., Bokuta, S. A., & Frantsevich, I. N. (1983). *Elastic constants and elastic moduli of metals and insulators handbook*. pp. 60–180. Kiev: Naukova Dumka.
- Gerday, A.-F. (2009). *Mechanical behaviour of Ti-5553 alloy modelling of representative cells* (Ph.D. Thesis). Liege, Belgium: University of Liege.
- Ghosh, A., Sivaprasad, S., Bhattacharjee, A., & Kar, S. K. (2013). Microstructure–fracture toughness correlation in an aircraft structural component alloy Ti-5Al-5V-5Mo-3Cr. *Materials Science and Engineering A*, 568, 61–67.
- Goedecker, S. (1997). Fast radix 2, 3, 4, and 5 kernels for fast Fourier transformations on computers with overlapping multiply–add instructions. *SIAM Journal on Scientific Computing*, 18(6), 1605–1611.
- Gonze, X. (1996). Towards a potential-based conjugate gradient algorithm for order- N self-consistent total energy calculations. *Physical Review B*, 54(7), 4383–4386.
- Gonze, X., Beuken, J. M., Caracas, R., Detraux, F., Fuchs, M., Rignanese, G. M., et al. (2002). First-principles computation of material properties: The ABINIT software project. *Computational Materials Science*, 25(3), 478–492.
- Gonze, X., Amadon, B., Anglade, P. M., Beuken, J. M., Bottin, F., Boulanger, P., et al. (2009). ABINIT: First-principles approach to material and nanosystem properties. *Computer Physics Communications*, 180(12), 2582–2615.
- Hohenberg, P., & Kohn, W. (1964). Inhomogeneous electron gas. *Physical Review*, 136(3B), B864–B871.
- Jones, N. G., Dashwood, R. J., Jackson, M., & Dye, D. (2009a). β Phase decomposition in Ti-5Al-5Mo-5V-3Cr. *Acta Materialia*, 57(13), 3830–3839.
- Jones, N. G., Dashwood, R. J., Jackson, M., & Dye, D. (2009b). Development of chevron-shaped α precipitates in Ti-5Al-5Mo-5V-3Cr. *Scripta Materialia*, 60(7), 571–573.
- Kohn, W., & Sham, L. J. (1965). Self consistent equations including exchange and correlations effects. *Physical Review A*, 140, A1133–A1138.
- Levinger, B. W. (1953). Lattice parameters of beta titanium at room temperature. *Journal of Metals*, 5, 195.
- Manda, P., Chakkingal, U., & Singh, A. K. (2014). Hardness characteristic and shear band formation in metastable β -titanium alloys. *Materials Characterization*, 96, 151–157.
- Manda, P., Ghosal, P., Chakkingal, U., & Singh, A. K. (2015). Effect of alloying elements in hot-rolled metastable β -titanium alloys: Part I. Evolution of microstructure and texture. *Metallurgical and Materials Transactions A*, 46(6), 2646–2663.

- Manda, P., Chakkingal, U., & Singh, A. K. (2016). Effect of alloying elements in hot-rolled metastable β -titanium alloys: Part II. Mechanical properties. *Metallurgical and Materials Transactions A*, 47, 3447–3463.
- Monkhorst, H. J., & Pack, J. D. (1976). Special points for Brillouin-zone integrations. *Physical Review B*, 13(12), 5188–5192.
- Nag, S. (2008). *Influence of beta instabilities on the early stages of nucleation and growth of alpha in beta titanium alloys* (Ph.D. Thesis). USA: The Ohio State University.
- Payne, M. C., Teter, M. P., Allan, D. C., Arias, T. A., & Joannopoulos, J. D. (1992). Iterative minimization techniques for ab initio total-energy calculations: Molecular dynamics and conjugate gradients. *Reviews of Modern Physics*, 64(4), 1045.
- Perdew, J. P., Burke, K., & Ernzerhof, M. (1996). Generalized gradient approximation made simple. *Physical Review Letters*, 77(18), 3685.
- Pugh, S. F. (1954). Relations between the elastic moduli and the plastic properties of polycrystalline pure metals. *London, Edinburgh, and Dublin Philosophical Magazine and Journal of Science*, 45(367), 823–843.
- Shekhar, S., Sarkar, R., Kar, S. K., & Bhattacharjee, A. (2015). Effect of solution treatment and aging on microstructure and tensile properties of high strength β titanium alloy, Ti-5Al-5V-5Mo-3Cr. *Materials & Design*, 66, 596–610.
- Takeuchi, A., & Inoue, A. (2005). Classification of bulk metallic glasses by atomic size difference, heat of mixing and period of constituent elements and its application to characterization of the main alloying element. *Materials Transactions*, 46, 2817–2829.
- Weiss, I., & Semiatin, S. L. (1998). Thermomechanical processing of beta titanium alloys – An overview. *Materials Science and Engineering: A*, 243(1), 46–65.